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Prediction and Measurement of Weld Dilution in Robotic CO2 Arc Welding

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Abstract: Weld dilution is an important feature of weld bead geometry that determines the mechanical and chemical properties of a welded joint. For robotic CO₂ arc welding, several welding process parameters are reported to be controlling the dilution. This paper investigates the relationship between four of these process parameters and dilution by depositing 'bead on plate' robotic CO₂ arc welds over mild steel plates. Two level four factor full factorial design method was used for conducting the experimental runs and linear regression models were developed accordingly. The adequacy of the models were tested by applying students 't' test and the predicted values from the models were plotted against the observed values through scatter diagram. Results showed that the proposed two level full factorial empirical models could predict the weld dilution with reasonable accuracy and ensure uniform weld quality. It can be concluded that robotic CO₂ arc welding is a very simple and effective tool for quantifying the main and interactive effects of welding parameters on dilution. Future works should focus in analyzing the influence of variable pure gasses as well as the gas mixture on dilution percentage in robotic arc welding.

Key words: Robotic CO₂Arc Welding % Process Control Parameters % Weld Dilution % Mathematical Modeling

INTRODUCTION

Weld surfacing is a metal deposition process in the form of a single or multiple layers over a basemetal, generally named as substrate. Based on the function, there are several classifications in surfacing process, namely a) hardfacing - the deposition to produce high wear resistance surfaces over a ductile base metal; b) cladding-to produce high corrosion resistant surfaces through deposition; c) buttering - a process of making chemically or metallurgically compatible surfaces; and d) the metal deposition to reconstruct and reuse the worn out parts [1].

Surfacing by fusion welding process has been increasingly becoming popular as it substantially saves some of the most imperative costs that involve men, machines, materials and manufacturing and has been evolved rapidly in recent years for a wide range of

industrial applications. These applications include from relatively smaller food processing plants to much bigger petrochemical, cement, fertilizer and nuclear power plants [2]. Although most of the conventional welding processes viz., shielded metal arc welding (SMAW), submerged arc welding (SAW), gas tungsten arc welding (GTAW), plasma arc welding (PAW), flux cored arc welding (FCAW), electroslag welding (ESW), oxyacetylene welding (OAW) and explosive welding are extensively employed by the industry [3], however gas metal arc welding (GMAW) is one of the most recognised and widely used process for all types of weld surfacing mainly due to its high productivity and ease of automization.

In general, the automized/robotic arc welding process has several means to sense and regulate the various,interdependant process control variables so as to ensure the process-product quality, productivity and

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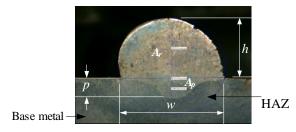


Fig. 1: Weld bead geometry related to dilution

the ensueing profitablity. The relationship between these process control variables and the resulting weld shape and weld bead geometry are inherently complex due to thenumber of variables involved and their inter-relationship on each other. The weld bead geometry (Figure 1), consists of several important features which include the weld width (w), weld penetration (p), weld reinforcement or weld height (h) etc., determines the quality of the weldment as well as the overall stress carrying capacity of the entire weld joint. Among many of these features of weld bead geometry, one of the most important is the weld dilution.

The dilutionpercentage, by definition is the ratio between the area of reinforcement (A_r) to the total area of weldment (A.). It is the single most important factor between a conventional welding of a joint and a weld surfacing, although surfacing is fundamentally a welding process. The weld bead geometry which determines the dilution, plays an important role in determining the mechanical properties of the weld [4-7]. To obtain the desired dilution, it is necessary to have a complete control over the related process control parameters so as to ascertain the relevant bead shape and geometry which would eventually determine the capacity of the weldment. Controlling of dilution is one of the major requirments for a successful weld surfacing process as the composition and properties of weld deposit have a very strong relationship with the dilution that prevails after welding. For cladding however, a low dilution is highly desirable as the final deposit composition needs to be closer to the corrosion resistant filler metal. There have been several attempts made by the researchers [8, 9], to investigate dilution in several fusion welding processes however, there are very little work done with robotic CO₂ process. The purpose of this paperis to develop mathematical models that define relationship between the process control parameters and dilution of bead on plate weldments made by using robotic CO2 arc welding process.

MATERIALS AND METHODS

Mathematical models, derived from the empirical datawhichare collected from statistically designed experiments [10-12], are generally intended by researchers to reduce the cost ofthe otherwise expensive yet exhausting "trial and error" methods. One of such models, based on the "factorial technique" isknown for simplicity and reasonable accuracy in predicting the relationship (generally linear), trend (direct or inverse) and magnitude of the main and interaction effects of control parameters involved over the response factors in question. There have been several other empirical data based statistical methods which are successfully used in order to understand the relationship between the process control parameters and the weld bead geometry [3-5].

For robotic CO₂ arc welding however, it is reported that the linear model obtained from the factorial technique is more effectively predicted the bead geometry than the curvilinear models which are otherwise increasingly becoming popular for several other fusion welding processes [5]. For the present study, atwo level fourfactor full factorial design of experiments technique is, therefore, employed with three replicated experimental develop linear mathematical Fourindividually controllable process control parameters such as welding current (I), rated voltage (V), arc travel rate (A) and electrode angle (W) are considered for dilution as the response parameter. All the direct and indirect parameters except the ones under consideration are kept constant. The upper limit (highest level) and the lower limit (lowest level) of a factor are coded as (+1) and (-1) or simply (+) and (-) respectively according to the equation (1).

$$X_j = \frac{X_{jn} - X_{jo}}{J_j} \tag{1}$$

Where, X_j is the coded value of the factor; X_{jn} is thenatural value of the factor; X_{j0} is thenatural value of the basic level; J_j is the variation interval and j is thenumber of the factors. Mild steel plates with 6mm in thickness were used as base material and "bead on plate" technique was applied for this study. The plates werethen cut into 150mm x 75 mm specimens and the surface of the plates were cleaned chemically and mechanically to remove any oxide or hydrogen presence on the welding surface. The selection of electrode wire, 0.8 mm diameter, AWS ER70S-6 was made based on

Table 1: Welding process control parameters and their limits

| - | | | | Limits | | | | |
|-------|-------------------|--------|----------|--------|------|--------|------|--|
| | | | | Actual | Code | Actual | Code | |
| Sl.No | Control Parameter | Unit | Notation | Low | Low | High | High | |
| 1 | Welding current | A | I | 180 | -1 | 260 | +1 | |
| 2 | Rated voltage | V | V | 18 | -1 | 26 | +1 | |
| 3 | Arc travel rate | cm/min | A | 24 | -1 | 46 | +1 | |
| 4 | Welding angle | degree | W | 90 | -1 | 145 | +1 | |

Table 2: Chemical composition of the welding wire

| | 1 0 | | | | |
|-------|------|------|--------------------------|--------------------------|------------|
| C | Mn | Si | $\mathbf{P}_{	ext{max}}$ | $\mathbf{S}_{	ext{max}}$ | Cu_{max} |
| 0.08% | 1.2% | 0.7% | 0.008% | 0.007% | 0.1% |

Table 3: Design matrix and responses

| - | Proces | s Control Pa | rameters | | | | | | | |
|----------|---------------|--------------|----------|----|---------------------|--------|--------|----------|--------|--------|
| Trial No | in coded form | | | | Response Parameters | | | | | |
| | I | V | A | W | At_I | At 2 | At 3 | $%D_{I}$ | D_2 | D_3 |
| 1 | -1 | -1 | -1 | -1 | 19.500 | 15.750 | 13.500 | 15.385 | 22.222 | 16.667 |
| 2 | 1 | -1 | -1 | -1 | 17.500 | 17.250 | 17.000 | 38.571 | 36.232 | 32.353 |
| 3 | -1 | 1 | -1 | -1 | 19.250 | 16.750 | 16.950 | 3.896 | 4.478 | 5.605 |
| 4 | 1 | 1 | -1 | -1 | 48.250 | 50.500 | 53.000 | 45.596 | 41.584 | 37.736 |
| 5 | -1 | -1 | 1 | -1 | 11.250 | 9.250 | 9.000 | 28.889 | 29.730 | 22.222 |
| 6 | 1 | -1 | 1 | -1 | 10.500 | 11.000 | 8.000 | 26.190 | 25.000 | 18.750 |
| 7 | -1 | 1 | 1 | -1 | 15.250 | 13.000 | 18.500 | 8.197 | 5.769 | 5.405 |
| 8 | 1 | 1 | 1 | -1 | 27.250 | 27.250 | 24.000 | 44.037 | 43.119 | 45.833 |
| 9 | -1 | -1 | -1 | 1 | 17.000 | 20.500 | 21.000 | 19.118 | 14.634 | 27.381 |
| 10 | 1 | -1 | -1 | 1 | 17.750 | 19.000 | 20.250 | 33.803 | 36.842 | 41.975 |
| 11 | -1 | 1 | -1 | 1 | 24.750 | 24.750 | 22.250 | 4.040 | 5.051 | 7.865 |
| 12 | 1 | 1 | -1 | 1 | 53.000 | 41.750 | 39.960 | 33.962 | 33.533 | 23.048 |
| 13 | -1 | -1 | 1 | 1 | 9.250 | 7.750 | 9.500 | 27.027 | 35.484 | 15.789 |
| 14 | 1 | -1 | 1 | 1 | 15.000 | 13.500 | 8.500 | 25.000 | 33.333 | 23.529 |
| 15 | -1 | 1 | 1 | 1 | 14.500 | 14.500 | 18.250 | 5.172 | 6.897 | 4.110 |
| 16 | 1 | 1 | 1 | 1 | 18.250 | 19.000 | 28.750 | 31.507 | 31.579 | 29.565 |

matching the mechanical and physical properties of the base metal and weld characteristics. While, the units, symbols and the limits of the factors (control parameters) are given in Table 1, the chemical composition of the electrode wire is given in Table 2.

The robotic CO₂ arc welding facility, OTC Daihen DR-4000, with a working range of 0-500A and 0-50V at the Faculty of Manufacturing engineering laboratory in Universiti Teknikal Malaysia Melaka (UTeM) was used for conducting the experiments as well as data collection. The shielding gas composition was kept at A_r 80% and CO₂ 20% for experimentation. A fixture was made to locate and fix the specimens on the machine table. The robot was turned on and with the shielding gas mixture turned on simultaneously, weld beads were made using bead on plate technique. Weld beads were deposited for a total length of 135 mm,as per the welding conditions prescribed by the design matrix. The welding robot and the experimental set up are shown in Figure 2.

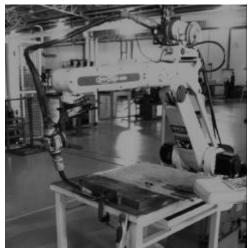


Fig. 2: Robotic GMAW machine at UTeM Facility

Since the full factorial technique prescribes 2ⁿ (n, number of control parameters) as the number of experimental runs and hence 2⁴, 16 experimental runs are

required for completing one set of DOE [12]. With three replications, there were totally 48 runs (3 16) required to fit each equation. Two sets of data were used to obtain the variance of optimization parameter and the third set was used to determine the variance of the adequacy of the model. To eliminate any systematic errors during the experiments, the experimental runs were randomized as per the table of random numbers. The detailed design matrix with observed response parameters for the three sets of experimental runs are given in Table 3.

The welded plates were checked for any visible defects and uniformity and then cross-sectioned at their axial midpoints to make test specimens. These 15 mm wide test specimens were metallurgically polished and etched with 5% nital solution. A reflective type profile projector was employed to trace the weldbead profiles of the test specimens and the bead geometry which includes penetration, reinforcement, width, area of penetration and the area of reinforcement was measured using a digital planimeter. The weld bead parameters that are related to dilution viz., area of reinforcement (A_r) and area of penetration (A_p) shown in Figure 1 were measured and the percent dilution (%D) was calculated by applying the formula as follows:

$$\%D = A_r/(A_r + A_p) \times 100 \tag{2}$$

The objective of this research was to predict the percentage dilution as a function of direct welding parameters such as arc current, rated voltage, arc travel rate and welding angle and can be written mathematically as

$$\%D = f(I, V, A, W) \tag{3}$$

The linear equation can be written in the form of a polynomial by taking into account all the possible two factor interaction:

$$\% D = \mathbf{b}_0 + \mathbf{b}_1 I + \mathbf{b}_2 V + \mathbf{b}_3 A + \mathbf{b}_4 W + \mathbf{b}_{12} I V + \mathbf{b}_{13} I A + \mathbf{b}_{14} I W + \mathbf{b}_{23} V A + \mathbf{b}_{24} V W + \mathbf{b}_{34} A W$$
(4)

Where %D is the measured dilution percentage, $\$_0,\$_1,\$_2,\$_3$ and $\$_4$ are the linear coefficients to be estimated which depend on the four process control parameters I,V,A and W.A standard statistical software package (Minitab 16) was used for the statistical analysis. Employing the least square method based regression analysis, the measured values from the experiments - the area of reinforcement (A_p) , area of penetration (A_p) and

Table 4: Estimated values of the significant coefficients of the models

| | Response parameters | | | | |
|-------------------------|---------------------|--------|--------|--------|--|
| Coeffi -cients | A _r | A_n | A_t | %D | |
| \$ ₀ | 14.937 | 5.679 | 20.617 | 24.871 | |
| \$ ₁ | 1.094 | 3.711 | 4.805 | 10.122 | |
| \$ ₂ | 4.437 | 1.695 | 6.133 | -3.095 | |
| \$ ₃ | -4.172 | -1.664 | -5.836 | - | |
| \$ ₄ | - | - | - | - | |
| \$ ₁₂ | 1.375 | 2.726 | 4.102 | 6.127 | |
| \$ ₁₃ | - | -1.570 | -1.867 | -3.084 | |
| \$ ₁₄ | - | - | - | - | |
| \$ ₂₃ | -1.484 | -0.805 | -2.289 | | |
| \$ ₂₄ | - | -0.758 | - | - | |
| \$ ₃₄ | -0.844 | - | - | - | |

Table 5: Analysis of variance (ANOVA) tests for mathematical models for dilution

| Standard | Coefficient of | Coefficientof |
|-------------------|--|--|
| error of estimate | multiple correlation | determination (%) |
| 0.336 | 0.981 | 96.37 |
| 0.299 | 0.971 | 94.33 |
| 0.791 | 0.950 | 90.26 |
| 0.750 | 0.966 | 93.36 |
| | error of estimate 0.336 0.299 0.791 | error of estimate multiple correlation 0.336 0.981 0.299 0.971 0.791 0.950 |

area of weldment (A_i) were analysed with dilution as response. A significance level of 5% on Fisher's F-ratio that represents the main and interactive effects of the individual control parameters shown to be important, the following equations were to be estimated:

$$A_r = 14.937 + 1.094I + 4.437V - 4.172A + 1.375IV - 1.484VA - 0.844AW$$
 (5)

$$A_p = 5.679 + 3.711 I + 1.695 V - 1.664 A +$$

$$2.726 IV - 1.57 IA - 0.805 VA - 0.758 VW$$
(6)

$$A_t = 20.617 + 4.805 I + 6.133 V - 5.836A + 4.102 IV - 1.867 IA - 2.289 VA$$
(7)

For the developed linear models, the adequacy of the models and the significance of each coefficients were tested by applying the analysis of variance (ANOVA) technique. The estimated values of each of the statistically significant linear coefficients, both individual and combinations of $\$_0, \$_1, \$_2, \$_3$ and $\$_4$ of the linear factorial regression models are given in Table 4.

The standard error of estimates (*SE*), coefficients of multiple correlations (R) and coefficients of determination (R²) made from the regression analysis are given in

Evidently from Table 5 it can be seen that the equations used to predict the dilution are adequate because of higher values of the coefficients of determination and lesser values of standard error.

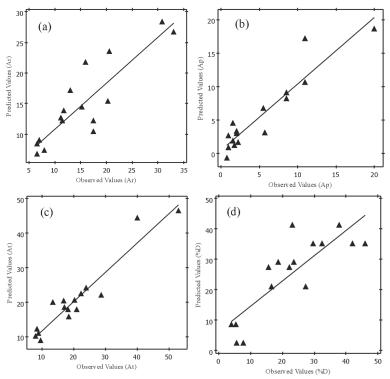


Fig. 3: Scatter diagram for a) Area of reinforcement (A_p) ; b) Area of penetration (A_p) ; c) Area of weldment (A_p) and d) Percentage dilution (%D)

The validity, accuracy and spread of the values of the developed models were scrutinized by plotting the results in scatter graphs. These graphs presented in Figure 3 show the predicted and observed values of the responses related to dilution using linear regression equations.

The results clearly demonstrate that the empirical data based linear mathematical models developed for the robotic CO₂ arc welding process could be able to have predicted a comparatively accurate percentage dilution with a reasonable confidence level of about 95%.

RESULTS AND DISCUSSION

The empirical data based mathematical models developed from the study can be used to predict the dilution control parameters by substituting the coded values of the respective process control parameters in the equations. The three response variables viz., A_p , A_p , and A_t , which were calculated from those models for each set of welding parameters I, V, A and W individually in their coded form are represented in equation 4 and 7 respectively. Subsequently, it is possible to obtain the required values of each of the process control parameters by simply substituting the values of the

desired dilution in the model. However, the factorial models of these three response variables and the influence of their respective process control parameters are beyond the scope of this paper and hence are not discussed. For the current discussion, A_p , A_p and A_t are merely used to calculate dilution percentage (%D) as per equation (1) and to recheck the validity and conformity of the developed regression models. Under prescribed welding conditions, the proposed empirical model for the prediction of %D after neglecting the statistically insignificant coefficients in the coded form is given by:

$$\% D = 24.871 + 10.122 I - 3.095 V + 6.217 I V - 3.084 IA$$
(8)

This empirical model could provide more useful information and possible guidelines for the robotic CO_2 arc welding system with a reasonable accuracy by analysing both the main and combined interaction effects of each of the individual process control variables on dilution. For a 2^k factorial based experiment, the effect of a controlling factor over a given response (Y) can be represented as:

$$E_A = \overline{Y}_{A+} - \overline{Y}_{A-} \tag{9}$$

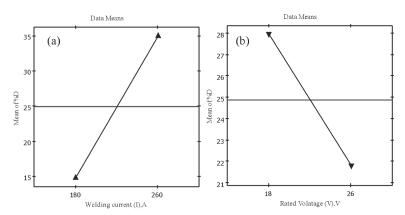


Fig. 4: Direct effects of process control parameters on dilution%D

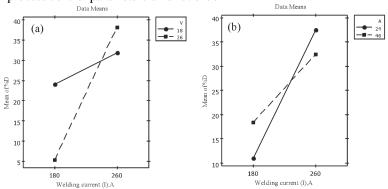


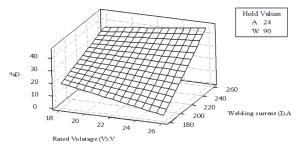
Fig. 5: Interaction effects plot for process control parameters on dilution%Da). %D Vs Welding current (I) and Rated Voltage (V); b) %D Vs Welding current (I) Arc travel rate (A)

Where E_A is the effect of A and \bar{Y}_{A+} , \bar{Y}_{A-} are the response data means obtained from experiments when effect A was kept at its lower and higher limit values respectively [12]. Based on this principle, it is evident from the model [equation (8)], that among the four process control parameters (I, V, A and W) considered, only welding current (I) and rated voltage (V) had direct effects on% Dwhile the other two control parameters, the arc travel rate (A) and the welding angle (W) were found to be statistically insignificant direct effects on the response. The model also indicated that the welding current hada direct relationship, while the rated voltage had an inverse relationship, each of them individually with the response, %D.

However, the welding current combined with the rated voltage had a positive interaction effect while its combination with the arc travel rate had an inverse interactive relationship with the dilution at both levels. For a better understanding, the % Dcomputed from the model with the highest coefficient of multiple correlationare plotted graphically as shown in Figure 4 and 8.

From Figure 4(a) an increase in welding current (from 180A to 260A) increases the dilution whereas the increase in voltage (from 18V to 26V) reduces it [Figure 4(b)]. It is well known that the heat input from the welding arc is controlled by welding current which means an increase in welding current increases the heat input and hence the melting rate, thereby increasing the dilution. On the other hand, an increase in voltage spreads the arc further and reduces the heat intensity by affecting the heat flux over the surface area under the arc. In general, both results are in total agreement with most of the published results based on several types of arc welding processes [5, 8]. The results also proved that the factorial technique is a simple yet very efficient and useful tool for understanding and evaluating the individual process parameters on dilution for robotic CO₂ arc welding. Figure 5 and 8 show the interaction effects of the process parameters with respect to the dilution.

A closer look at the interaction effects plotted in Figure 5 reveals that when the welding current interacts with rated voltage [Figure 5(a)], as well as the arc travel rate [Figure 5(b)], has a direct relationship with dilution.



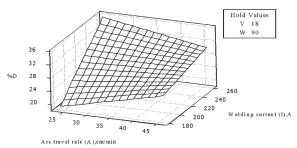


Fig. 6: Interaction effects plot for Rated Voltage (V) and Welding current (I) on dilution

Fig. 7: Interaction effects plot for Arc travel rate (A) and Welding current (I) on dilution

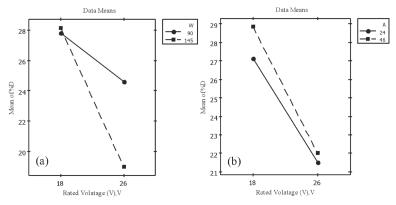


Fig. 8: Interaction effects plot for process control parameters on dilution%Da)%D Vs Rated voltage (V) and Welding angle (W); b) %D Vs Rated voltage (V) and Arc travel rate (A)

It is interesting to note that in robotic CO₂ arc welding the rated voltage individually has an inverse relationship in determining the dilution however, combined with welding current it has a direct interaction effect over dilution. Moreover, evidently from the plot in Figure 5(a), the influence of welding current on dilution is very prominent when the rated voltage is at its higher level, 26 V. For a better understanding of the interaction effect of the statistically significant process parameters, surface plots are also drawn and shown in Figure 6 and 7.

The surface plot shown in Figure 6 confirms the results further that the welding current and voltage has a very strong interaction effect on dilution in robotic CO₂ arc welding. It is also interesting to note that the surface plot has indicated that an increase in rated voltage at a low current level has a slightly negative effect. This phenomenon exists because of the fact that the high voltage generally spreads the arc further and when combined with low current, it will affect the melting rate as well as the convection heat flow, resulting in changes in metal flow within the weld puddle. While analyzing the interaction plot shown in Figure 7 and 5(b), the welding current and arc travel rate have

positive interaction effect over weld significant dilution. On the other hand, the influence of welding current on dilution is prominent when the arc travel rate is at a low level, 24 cm/min. The possible reasons could be due to the fact that the slower the arc moves over the base metal, the better the melting rate of both the base metal and electrode and so is the dilution. However, a closer look at the surface plot shown in Figure 7 indicates that an increase in arc travel rate has an inverse effect on percentage dilution. As the arc moves faster over the base metal, the rate of heat flow over the surface area of the metal will be reduced, resulting in a lesser melting rate and dilution. The interaction effects of rated voltage with welding angle and the arc travel rate are shown in Figure 8(a) and (b).

Although the increase in voltage has an inverse effect on dilution at both low and high levels of welding angle the reduction of percentage is more prominent when the angle was less acute, 145 degree. The possible reason for this particular state is that when the arc is directed to the base material at such a higher deviations from the vertical axis, it invariably affects the heat intensity over the surface of exposure and affects the melting rate considerably. However, the rated voltage

does not have significant interaction effect with the arc travel rate as shown from the statistical results and the plot in Figure 8(b).

CONCLUSION

Mathematical models were developed in order to predict weld dilution as a function of four process parameters that can be independently controlled and a robotic CO₂ arc during measured process. The developed models were able to predict process control parameters required to achieve desired dilution with 95% confidence level. The models can also be used to calculate other weld responses that are related and dependent on dilution and could assist the development of automatic welding control systems as well as expert systems so as to establish guidelines and criteria for the most effective weld surfacing design. Since the shielding gas plays an important role in determining the dilution in arc welding in general, there was only one combination of shielding gas mixture (A_r 80% and CO₂ 20%) which was investigated in this study due to the practical and financial limitations. Future worksshouldfocus in analyzing the influence of variable pure gasses as well as the gas mixture on dilution percentage in robotic arc welding.

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