# A Comparative Study of Small Scale Industries Involving with and Without Shortages 

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#### Abstract

In this paper, we develop an economic order quantity inventory model for various items which will minimize the total inventory cost. The study took place at a small business scale of industries (Fitness Gym). This paper takes into consideration of two cases like shortage and no shortage. In both cases total annual inventory costs for various items are calculated. The results obtained for various items are summarized which shows that the optimum cost in both case.


$\underline{\text { Key words: Inventory • EOQ • Shortage • Small scale industries }}$

## INTRODUCTION

Inventory plays a vital role for running the activities of every organization. It helps to improve the production and distribution process both are linked by inventory. Current asserts and working capitals need the investment in inventories. It gives enhancement of the organization. Thus it is very important and to have proper control and management of inventories. Ordering in right quantities at right time is always a crucial issue in many small scale industries because demand is uncertain and difficult to forecast.

Aghezzaf et al. [1] developed distribution and inventory management in supply chains of high consumption products. Chien et al. [2] studied an integrated inventory allocation and vehicle routing problem. Padmanabhan and Whang [3] analyzed information distortion in a supply chain: the bullwhip effect. Muniappan et al. [4] developed a production inventory model for vendor-buyer coordination with quantity discount, backordering and rework for fixed life time products. Muniappan et al. [5] analyzed an EOQ model for deteriorating items with inflation and time value of money considering time-dependent deteriorating rate and delay payments. Parlar [6] developed probabilistic
analysis of renewal cycles: An application to a non Markovian inventory problem with multiple objectives. Ravithammal et al. [7] studied an integrated production inventory system for perishable items with fixed and linear backorders. Ravithammal et al. [8] developed a deterministic production inventory model for buyermanufacturer with quantity discount and completely backlogged shortages for fixed life time product.

The rest of the paper is organized as follows: In section 2, assumptions, notations and model formulation of with and without shortages are given. In section 3 conclusions are given. Finally summary are presented.

## Model Formulation

Assumptions:

- Demand rate D is uniform and known.
- Lead time is zero.
- $\quad h, s$ denotes holding cost and shortage cost per order respectively.
- $c_{s}$ denotes ordering cost per order.
- $Q, Q_{s}$ denotes EOQ for without and with shortage respectively.
- $T C, T C_{s}$ denotes total cost for without and with shortage respectively.

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Table 1: Summary of solution of without shortage

| Items | Setup Cost | Demand | Holding Cost | $Q$ | TC |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Tread Mill | 102000 | 20320 | 32000 | 359.9 | 1151733.02 |
| Elliptical | 86000 | 24150 | 1800 | 480.38 | 8646872.266 |
| Spin Bike | 48000 | 27980 | 8000 | 589.711 | 4717694.352 |
| Upright Bike | 42000 | 8625 | 7000 | 321.71 | 2251999.111 |
| Recumbent Bike | 46000 | 14490 | 8200 | 403.20 | 3306244.99 |
| Rowing Machine | 75000 | 14490 | 36000 | 425.5878 | 5107053.945 |
| Functional Training | 120000 | 14490 | 36000 | 310.805 | 11188944.592 |
| Multi functional Bench | 17000 | 20320 | 4000 | 415.595 | 1662383.830 |
| Hype Extension | 15000 | 9660 | 8200 | 187.993 | 1541544.679 |
| Abdominal Bench | 12000 | 24150 | 4000 | 380.657 | 1522629.30 |
| Four Station | 95000 | 24840 | 12000 | 627.136 | 7525636.185 |
| Dumb bells | 160 | 24840 | 4000 | 43981 | 175927.257 |
| Aerobic Steps | 4500 | 54150 | 300 | 269.165 | 807496.1300 |
| Ankle Weight | 650 | 20320 | 1500 | 132.7051 | 199057.780 |
| Andicine Ball | 1300 | 9660 | 1100 | 151.1050 | 166215.522 |
| Gym Ball | 1499 | 20320 | 1500 | 201.526 | 302289.6624 |
| Resistance Tube | 1500 | 20320 | 4000 | 123.450 | 493801.579 |
| B Ball | 7990 | 24150 | 1500 | 507.228 | 76838.6819 |
| F Roller | 3500 | 9660 | 1100 | 247.93 | 272730.6363 |

Table 2: Summary of solution of with shortage

| Items | Setup Cost | Demand | Holding Cost | Shortage Cost | $Q_{S}$ | $T s_{s}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tread Mill | 102000 | 20320 | 32000 | 200 | 14427.03 | 907, 693.008 |
| Elliptical | 86000 | 24150 | 1800 | 250 | 4104.37 | 1, 012, 039.849 |
| Spin Bike | 48000 | 27980 | 8000 | 350 | 2875.89 | 965, 874.243 |
| Upright Bike | 42000 | 8625 | 7000 | 300 | 1586.97 | 456, 527.99 |
| Recumbent Bike | 46000 | 14490 | 8200 | 300 | 2146.195 | 621, 135.27 |
| Rowing Machine | 75000 | 14490 | 36000 | 250 | 2979.06 | 729, 579.135 |
| Functional Training | 120000 | 14490 | 36000 | 200 | 4181.45 | 831, 671.418 |
| Multi functional Bench | 17000 | 20320 | 4000 | 100 | 2661.07 | 259, 620.732 |
| Hype Extension | 15000 | 9660 | 8200 | 250 | 1092.93 | 265, 153.745 |
| Abdominal Bench | 12000 | 24150 | 4000 | 100 | 2437.34 | 237, 794.7465 |
| Four Station | 95000 | 24840 | 12000 | 250 | 4344.925 | 1, 075, 090.883 |
| Dumb bells | 160 | 24840 | 4000 | 50 | 401.202 | 19, 812.45 |
| Aerobic Steps | 4500 | 24150 | 3000 | 40 | 2346.4 | 92, 626.158 |
| Ankle Weight | 650 | 20320 | 1500 | 50 | 738.870 | 35,751.832 |
| Andicine Ball | 1300 | 9660 | 1100 | 40 | 806.67 | 31, 153, 0200 |
| Gym Ball | 1499 | 20320 | 1500 | 50 | 1122.04 | 54, 292.826 |
| Resistance Tube | 1500 | 20320 | 4000 | 50 | 1111.05 | 3491704.450 |
| B Ball | 7990 | 24150 | 1500 | 50 | 2846.79 | 135, 561.79402 |
| F Roller | 3500 | 9660 | 1100 | 50 | 492.867 | 56, 868.268 |

Case i EOQ Without Shortage: The ordering quantity which minimizes the balance of cost between the inventory holding cost and ordering cost is known as economic ordering quantity. Without shortage, order quantity and optimum total cost is given as follows: The order quantity is defined as $Q=\sqrt{\frac{2 D c_{S}}{h}}$ and the and
optimum total cost is given as $T C=\sqrt{2 D h c_{s}}$.

Case ii EOQ with Shortage: In this case, the order quantity is defined as $Q_{S}=\sqrt{\frac{2 D c_{s}(h+s)}{h s}}$ and the optimum total cost is given as $T C_{S}=\sqrt{\frac{2 D h s c_{S}}{(h+s)}}$.

## CONCLUSION

This paper focus on a comparative study of small scale industries involving with and without shortages. In both cases economic order quantity and optimal cost is developed. The goal of the model is to find the optimal EOQ which minimize the total inventory cost. In both cases the optimal results are summarized for various items which show the optimum annual total cost.

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